

# A Data Assimilation Approach to Solving the Coupled Ring Current Radiation Belt System

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# Model Types

## Purely Empirical

- exactly represent average of large data sets
- limited consistency with physical equations
- difficult/impossible to extrapolate

## Data Assimilation

- use all available observations + physical knowledge to constrain the model dynamics
- fidelity to physical equations and observations
- can provide cognitive synthesis + physical understanding + practical application

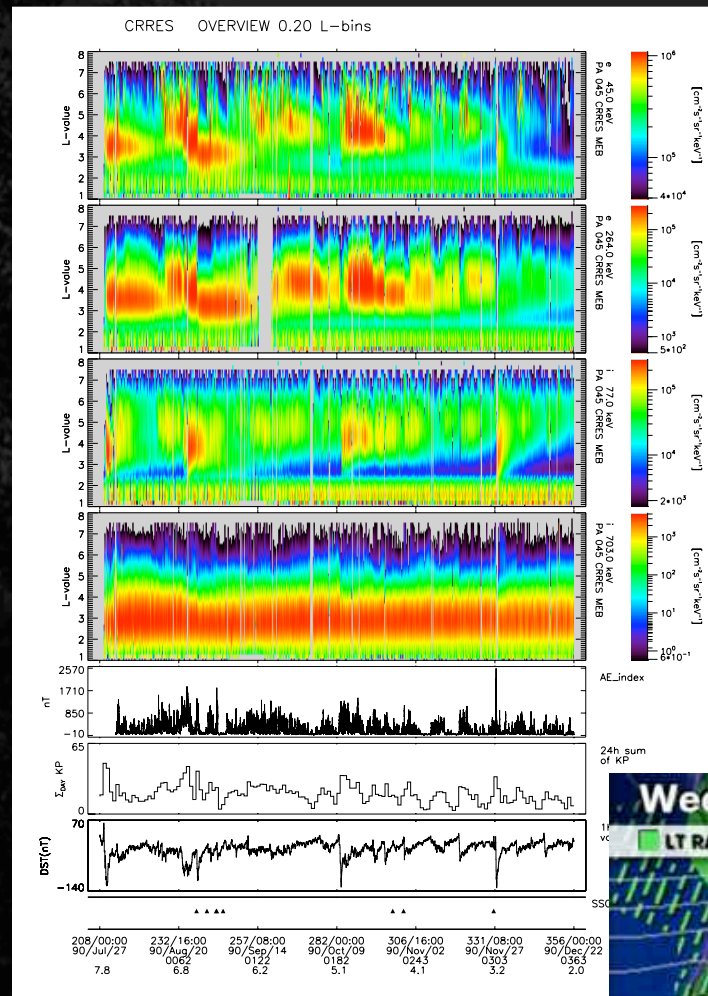
## Physics-Based Models

- limited ability to incorporate or match observations
- detailed physics and theory

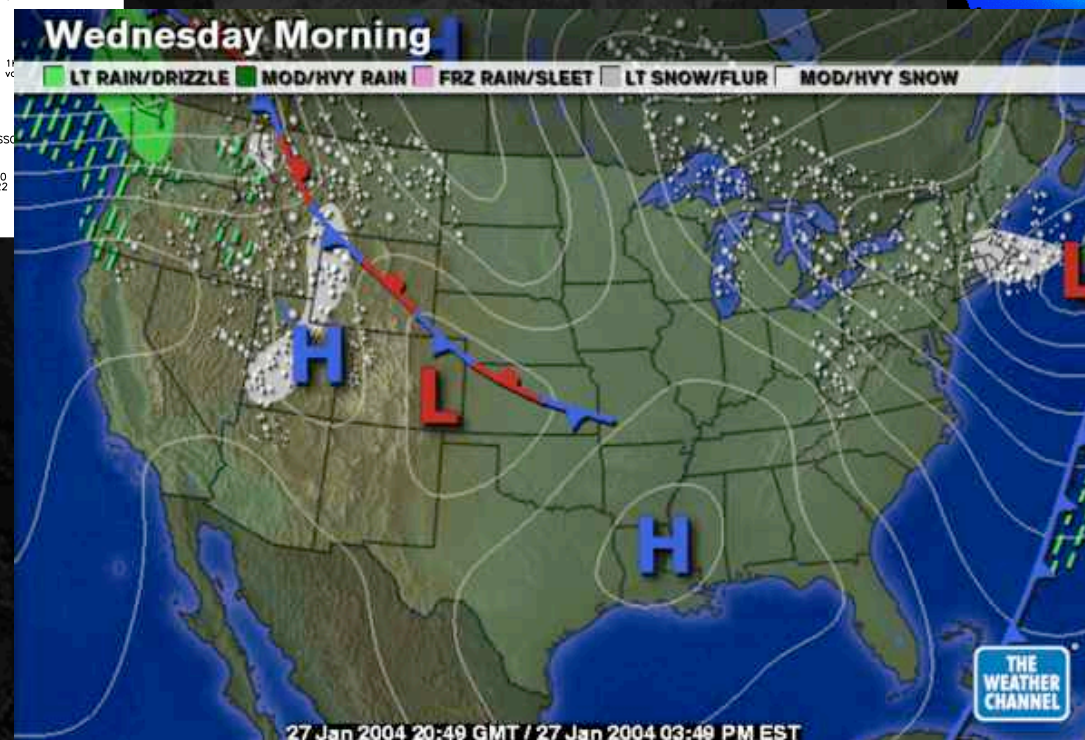
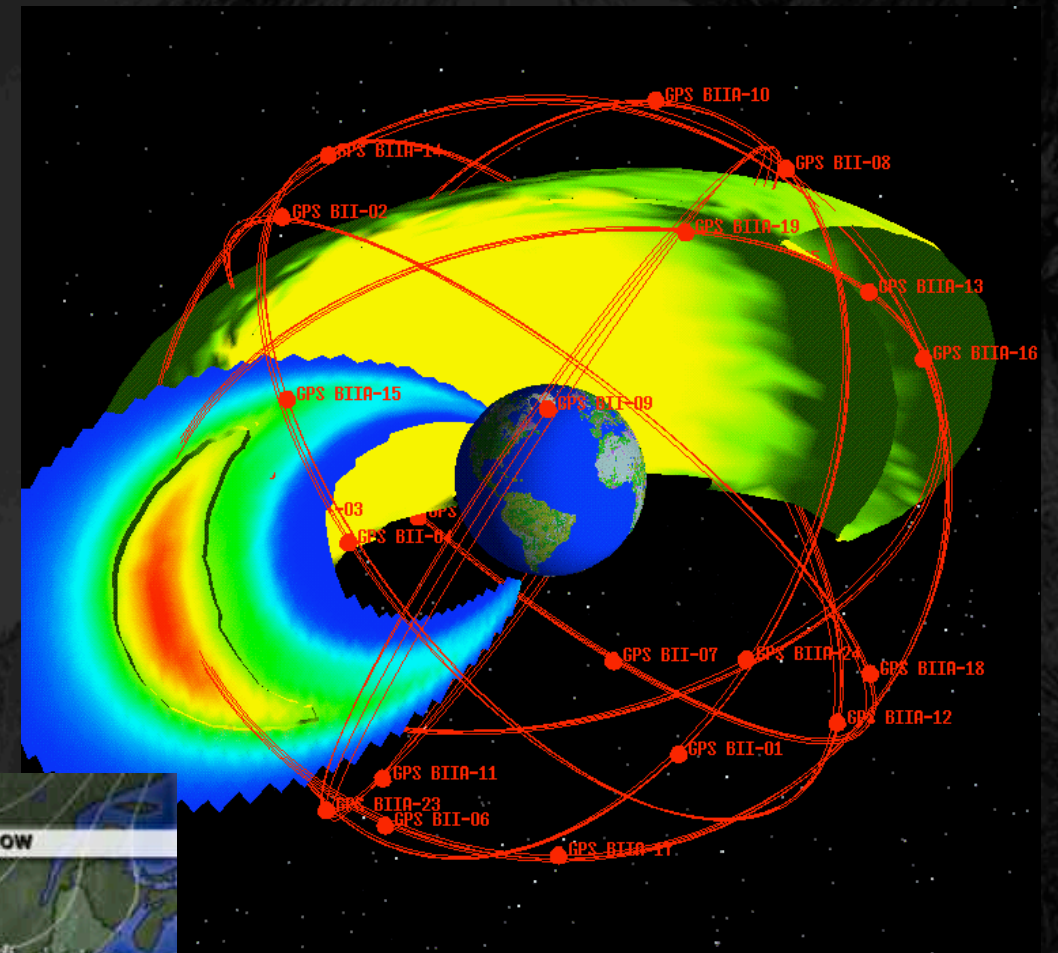


# Cognitive Synthesis

Multi-Dimensional Data



30+ Satellites



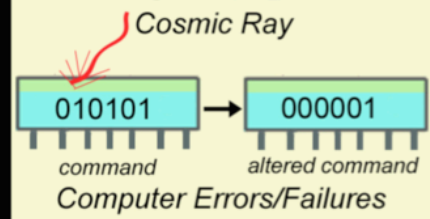
Cognitive Synthesis



# Practical Application

## Radiation Damage to Satellites

### Single Event Upset (SEU)

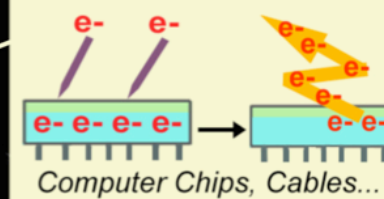


### Surface Charging

High-Energy  
Electron Flux

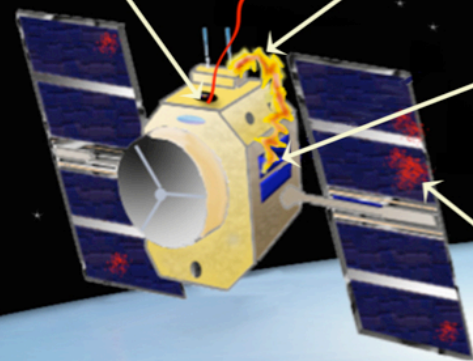
### Deep Dielectric Charge & Discharge

Radiation Belt Electrons



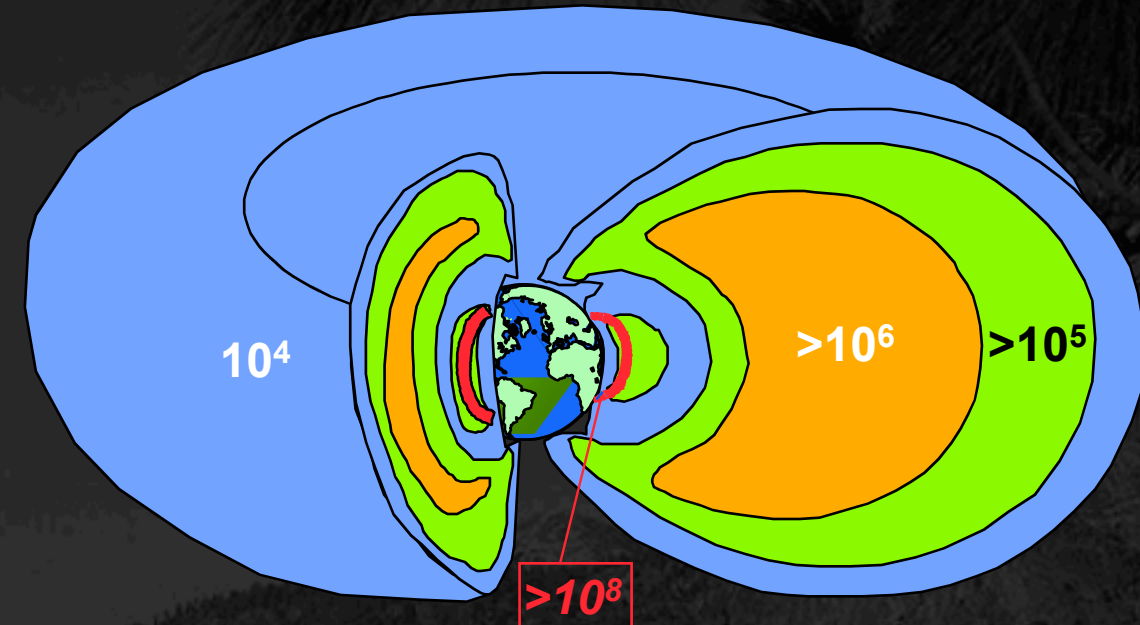
### Solar Panel Degradation

Solar Energetic Particles, Micro-meteoroids...

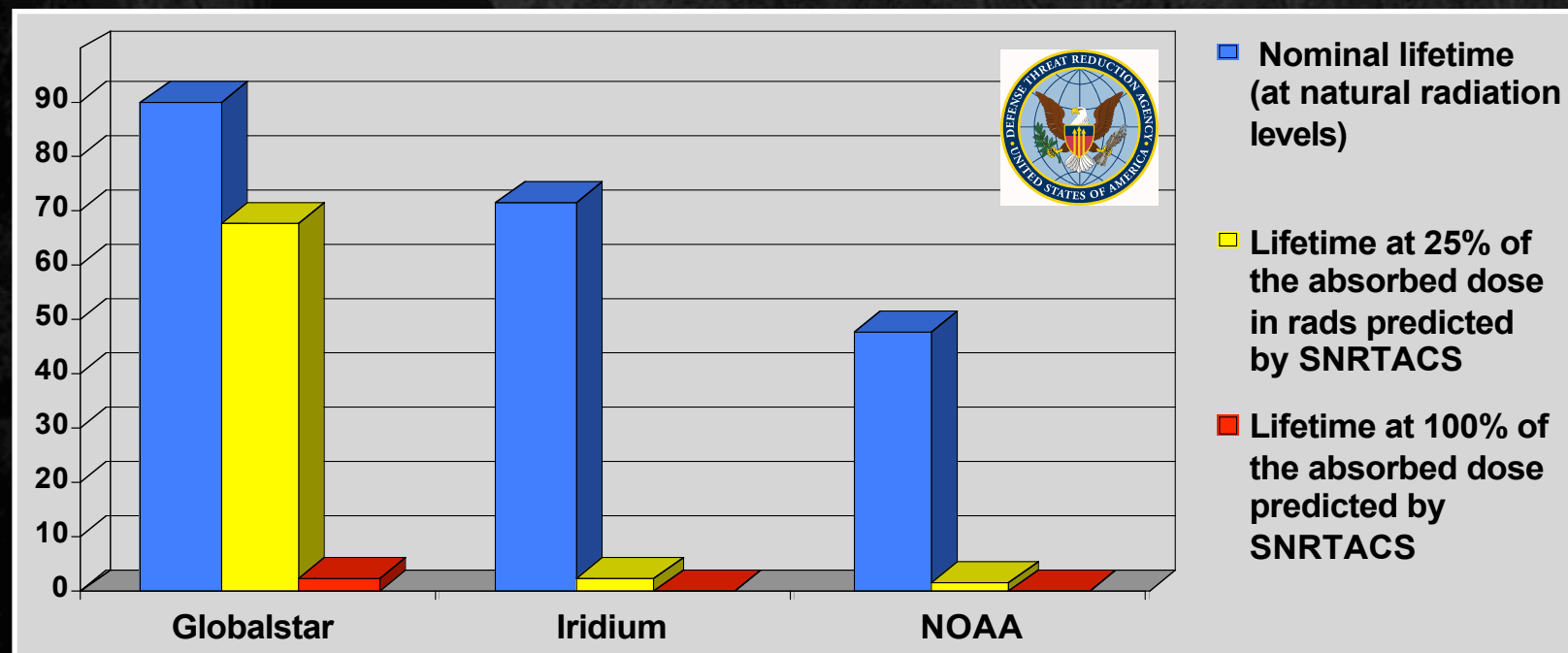


artwork by Dave Bouwer

## Natural and Enhanced Electron Population One Day After Burst Over Korea



Explosion-excited region

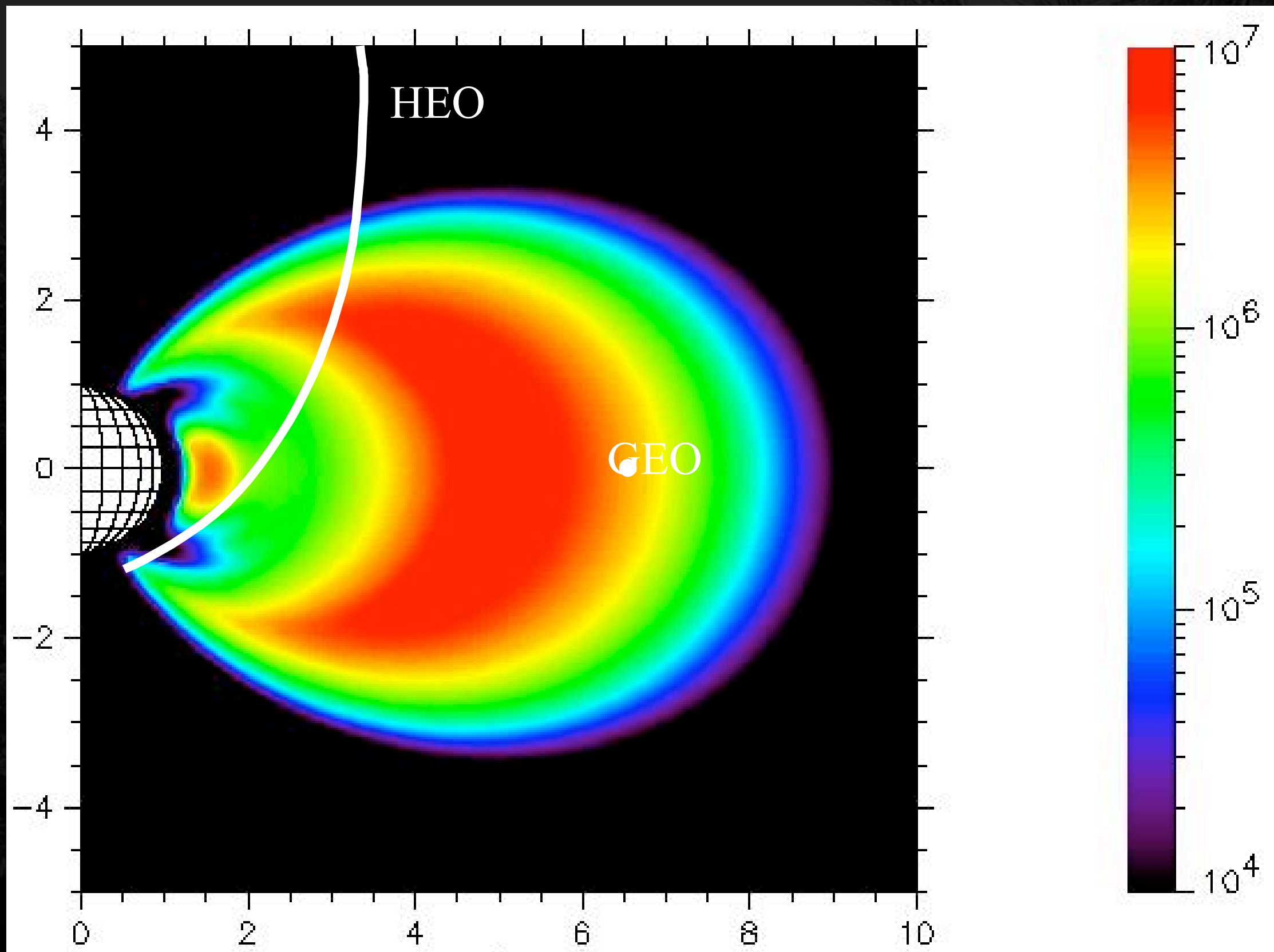


DTRA HALEOS Study  
April 2001



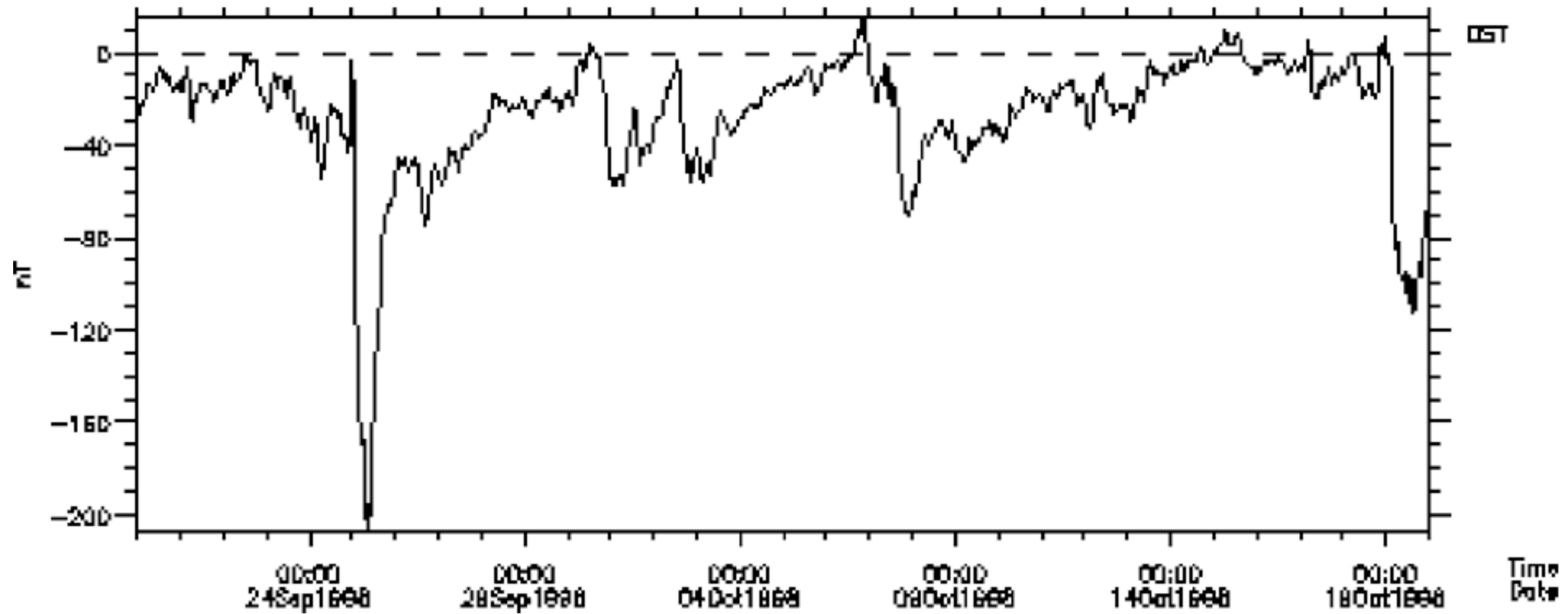
# Physical Understanding

- Diffusion Rates:  
Radial, Pitch Angle, and Energy
- Adiabatic Effects:  
quantify the effects of the ring current
- Loss Rates:  
quantify the temporal & spatial dependence
- Stochastic Processes:  
when, where, how strong?

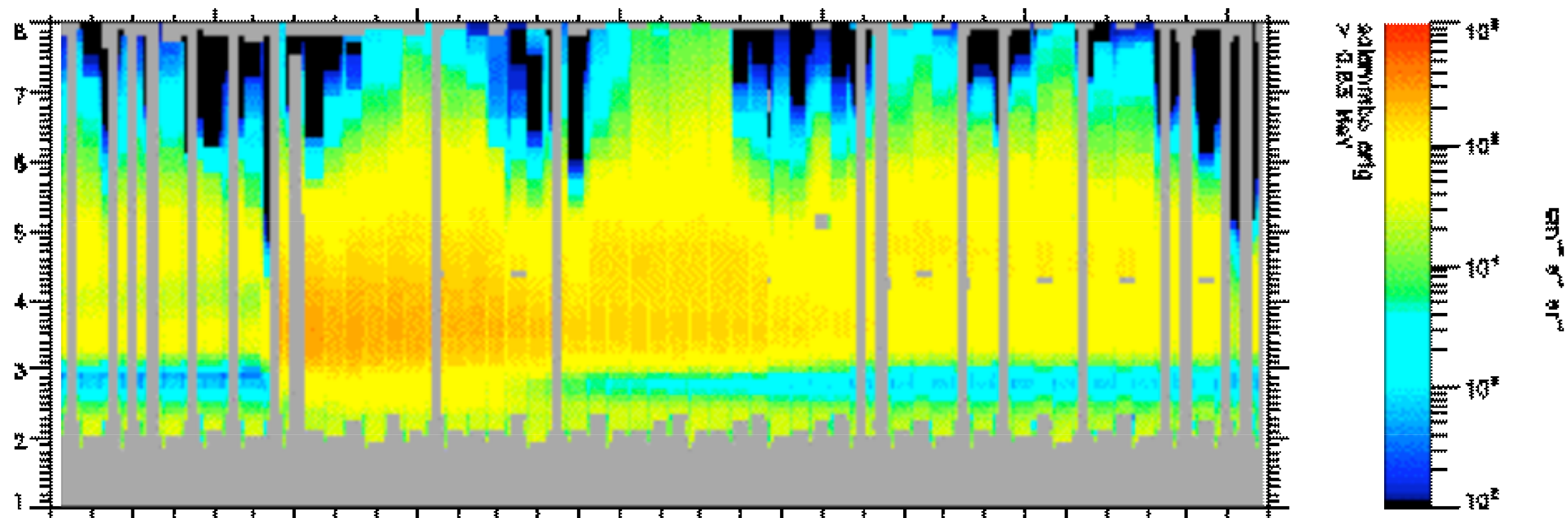




# One Month of Storms

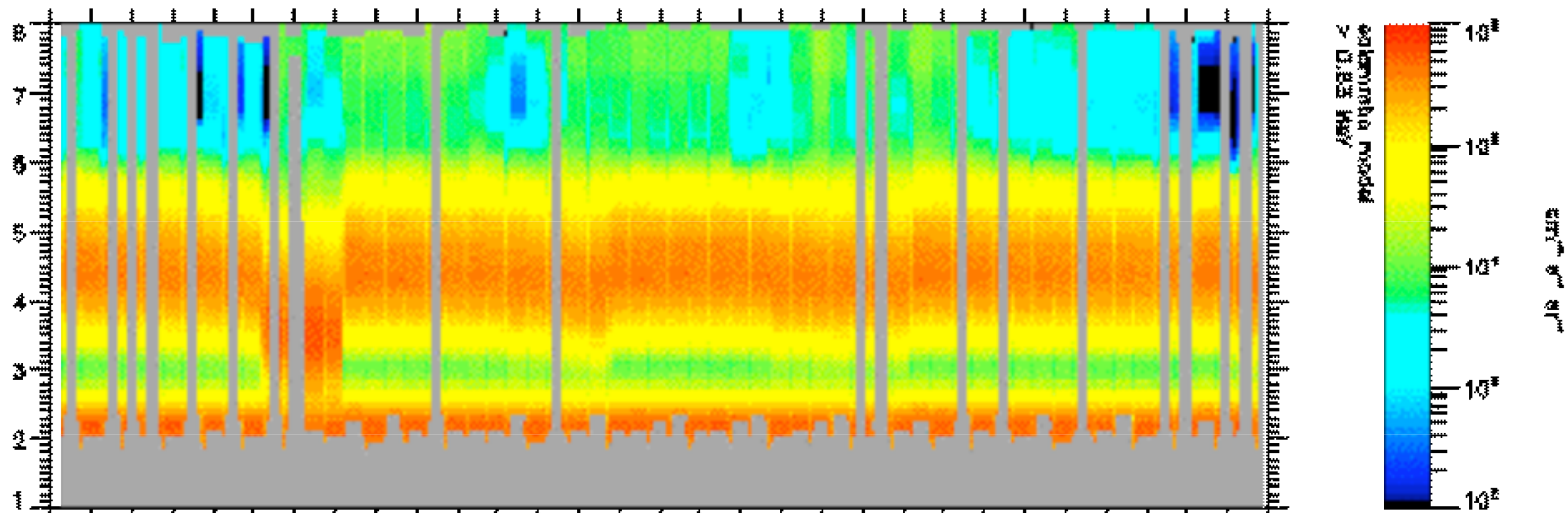


# Measured Flux vs L

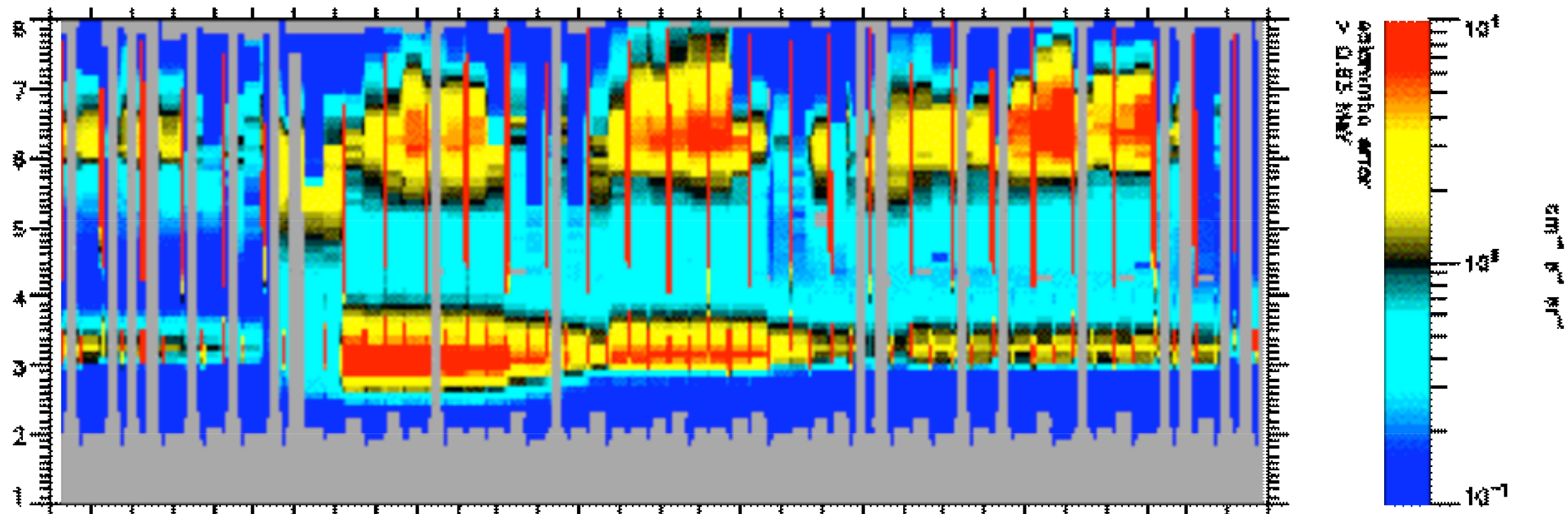




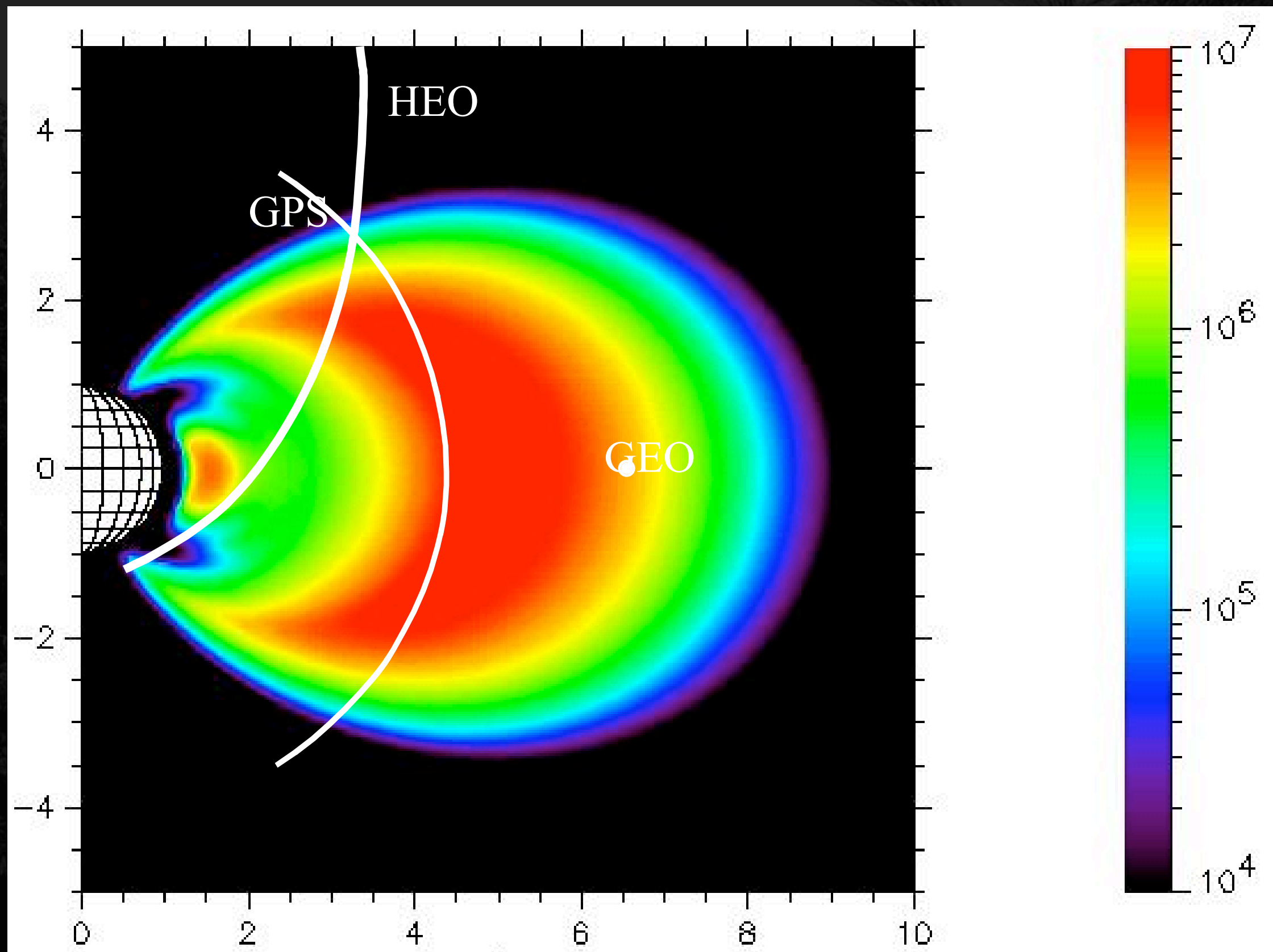
# Model Flux vs L



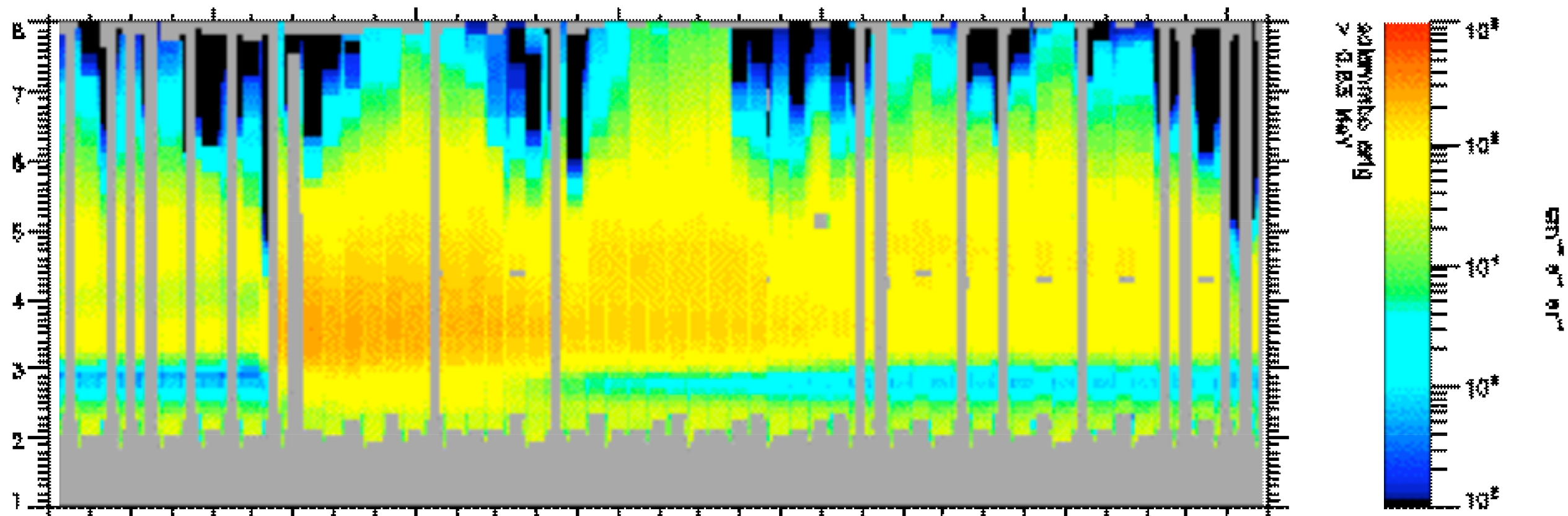
# Ratio of Measured/Model





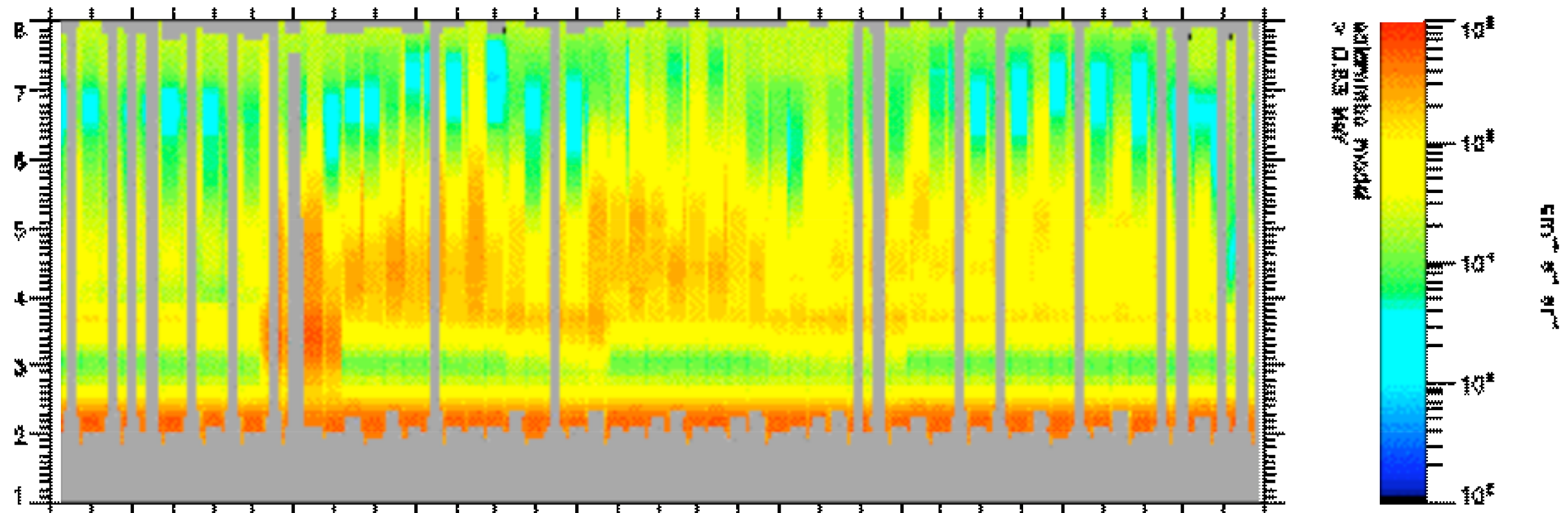


# Measured Flux vs L

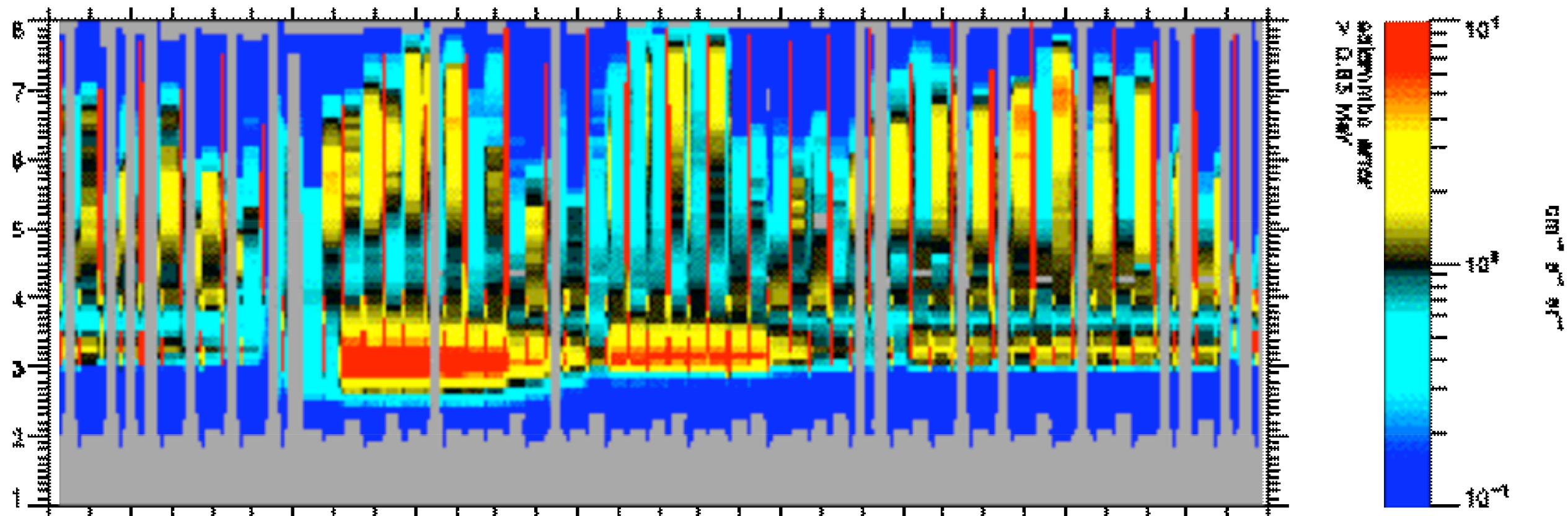




# Model Flux vs L



# Ratio of Measured/Model

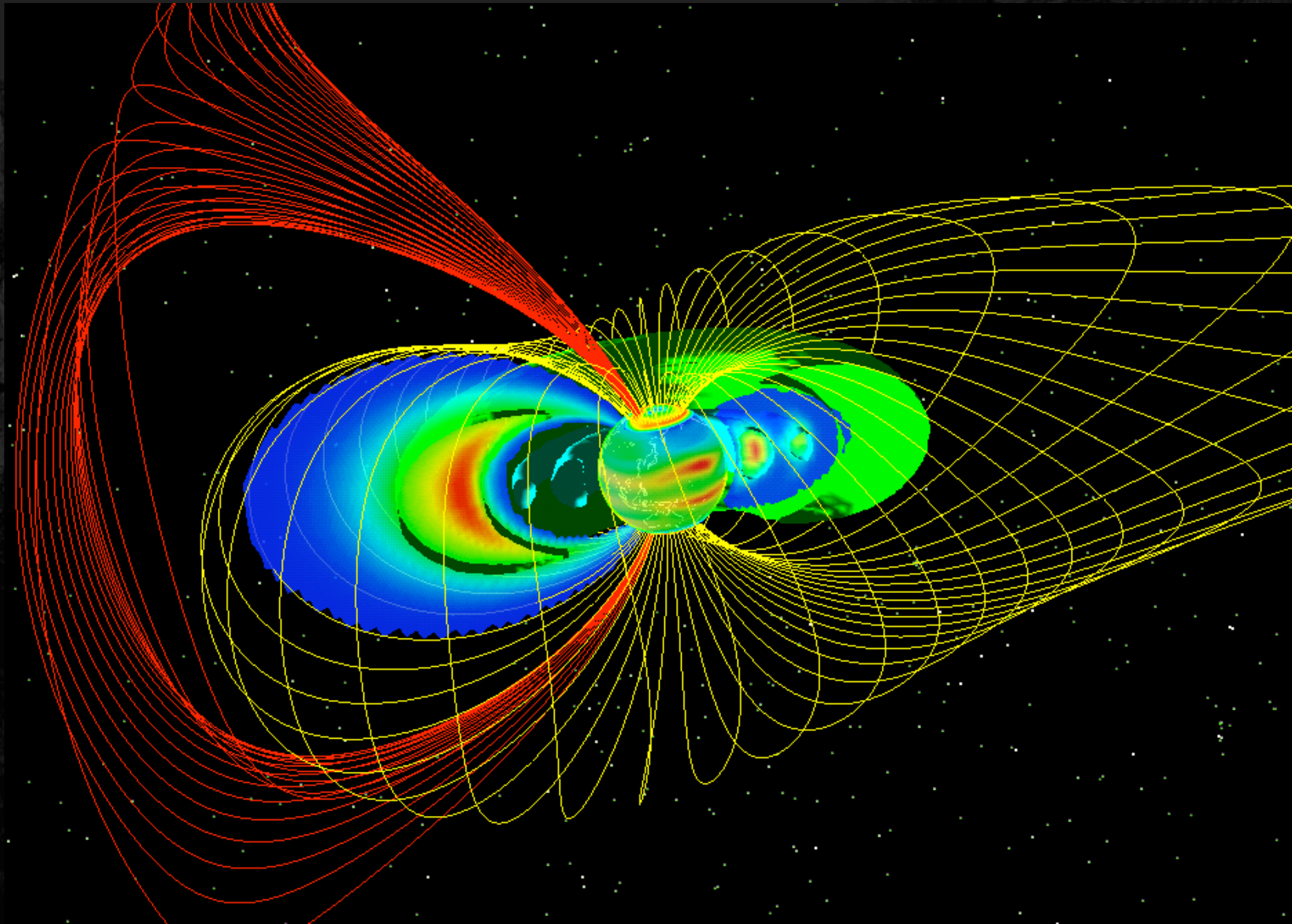




# Next Steps

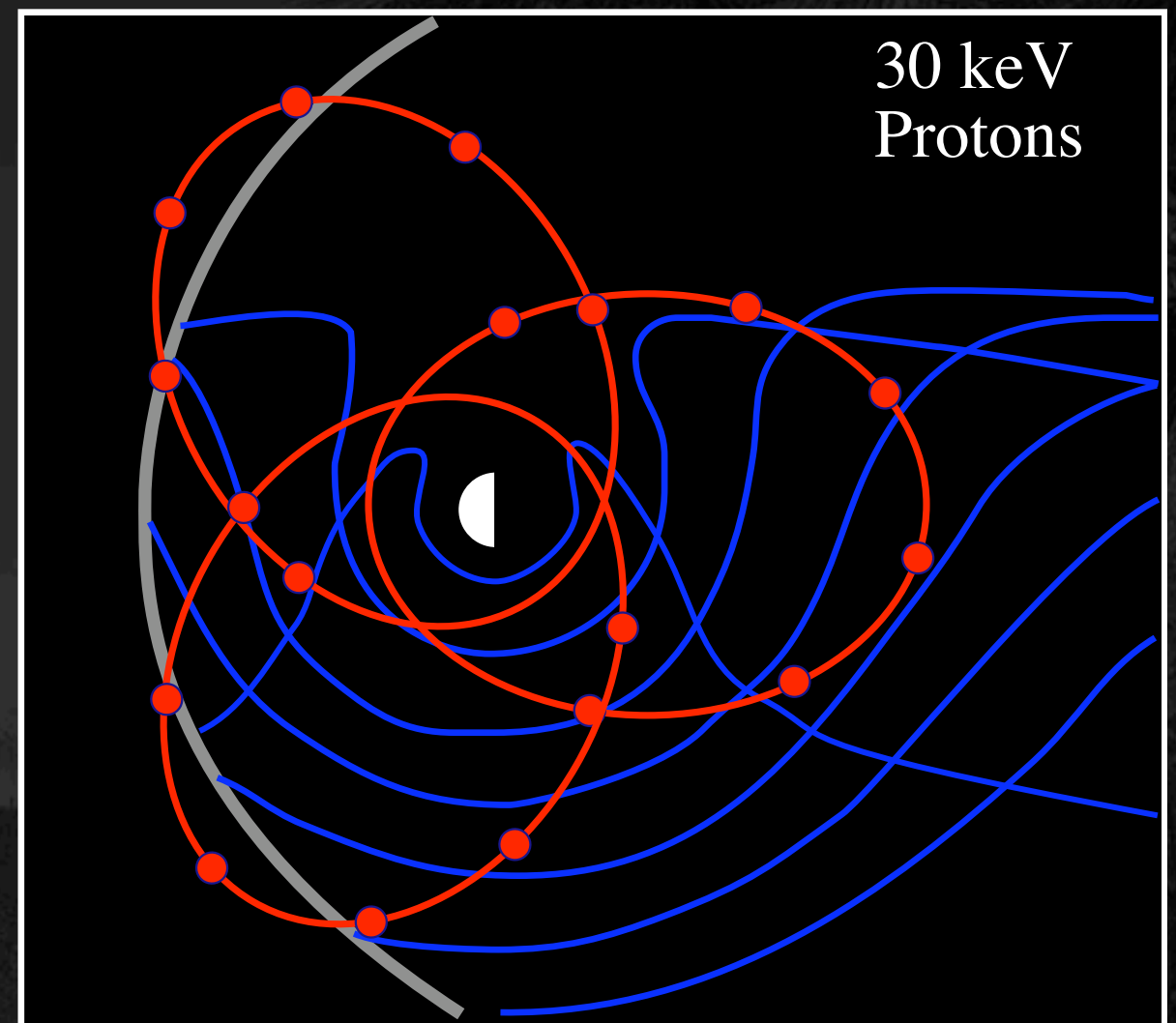
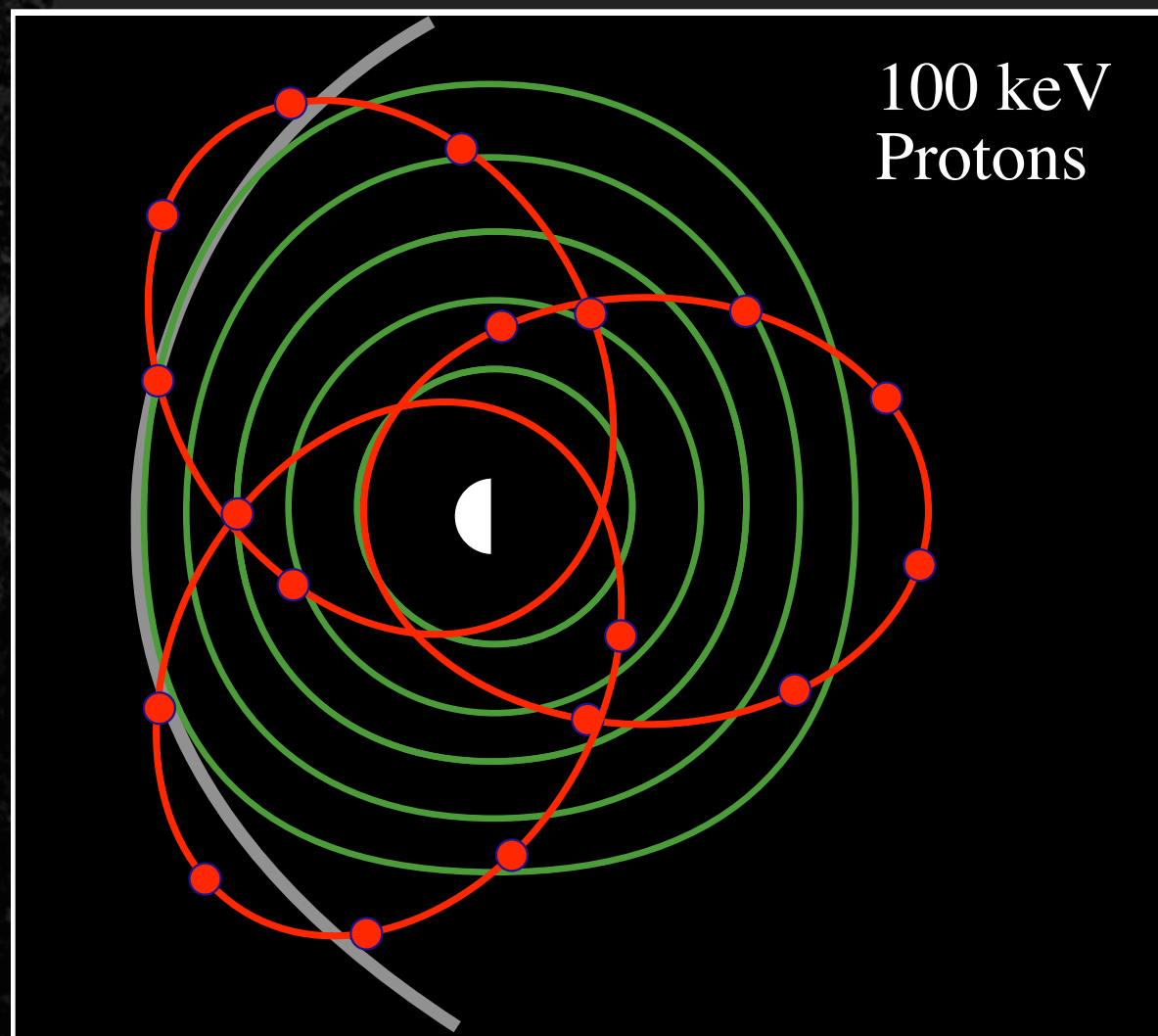
- Allow adjustable, time dependent diffusion rates
- Calculate diffusion rates through storm consistent with observations

# Solving Particles & Fields

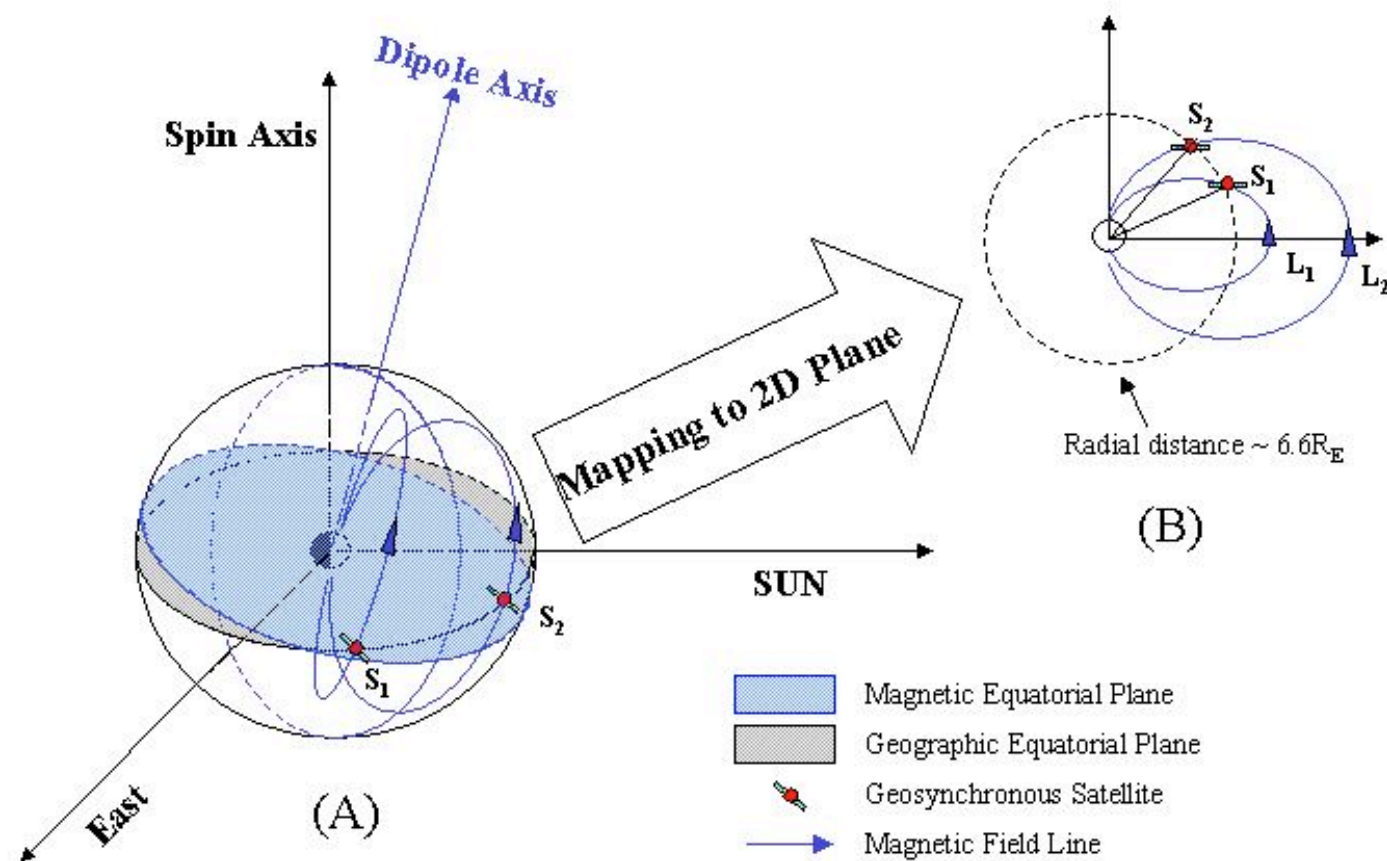




# Using Liouville's Theorem



- Phase space density conserved along a path
- Drift shell splitting actually helps!
- A single field must be consistent
- Low energies remotely sense E as well as B

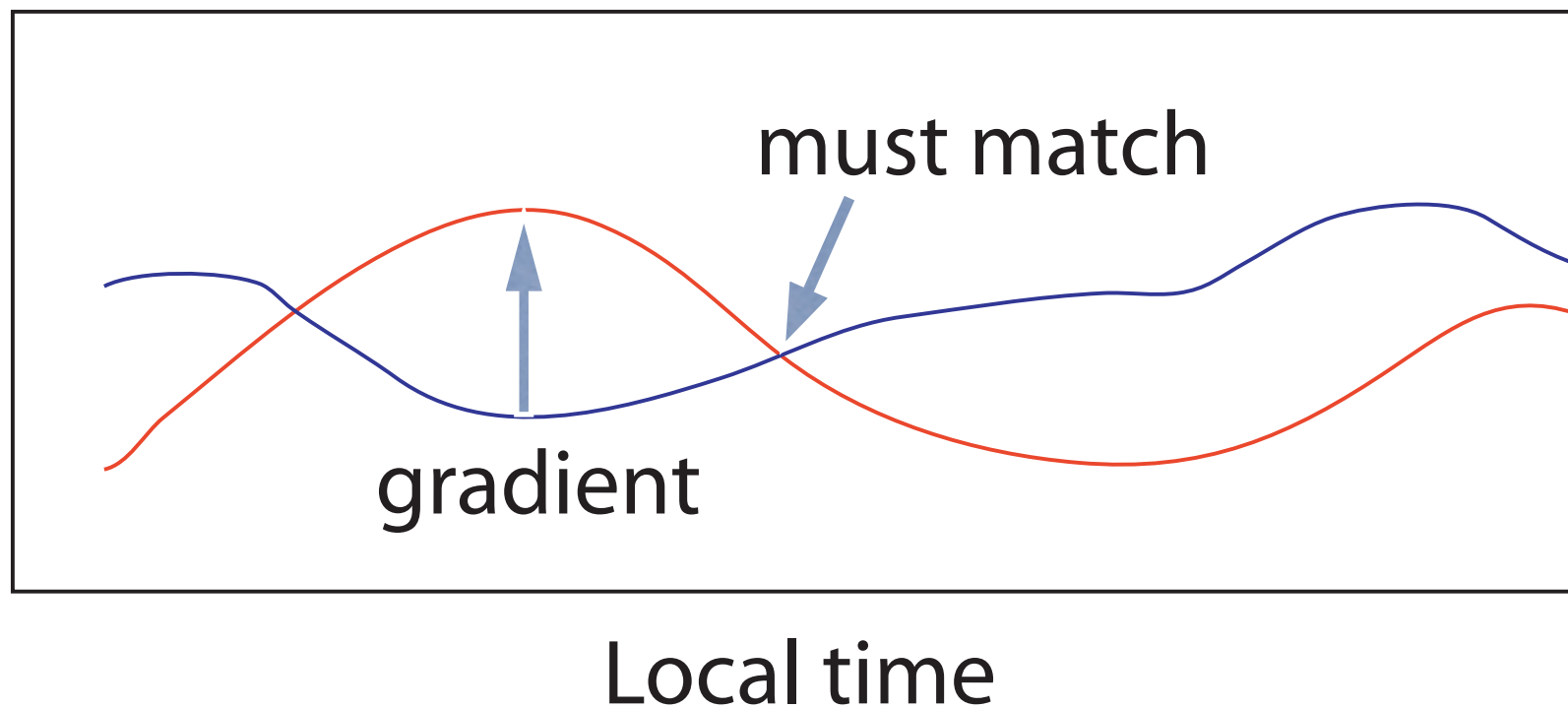


$\vec{B}$  from GOES  
 $\hat{B}$  from LANL

$\mu$  from B &  
 Energy Spectrum

J &  $L^*$  from B model

$L^*$  at fixed  $\mu$  and J



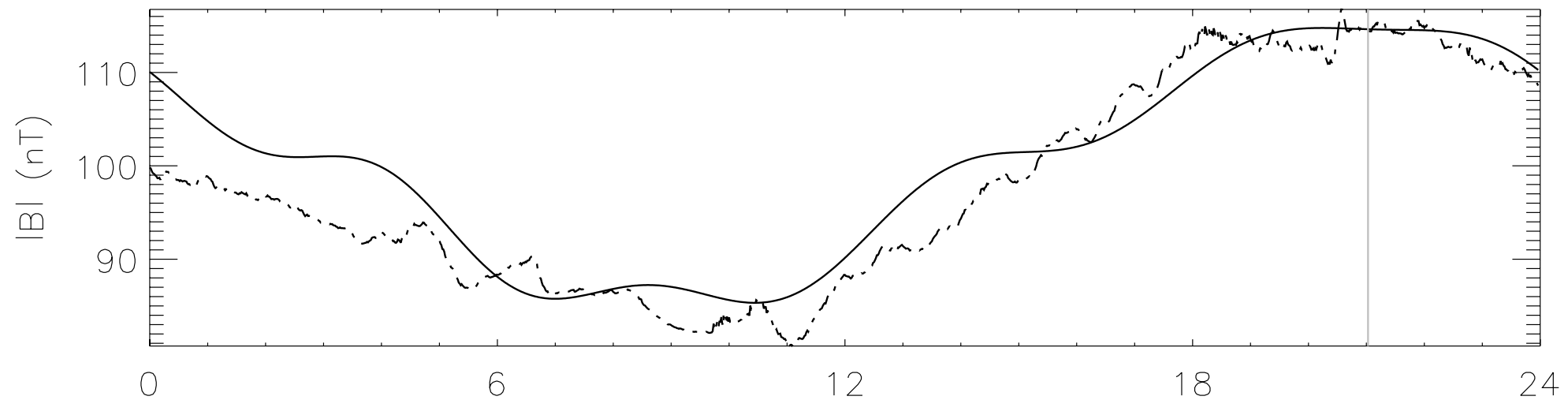
PSD at fixed  
 $\mu, J, L^*$



# Application to Quiet Days

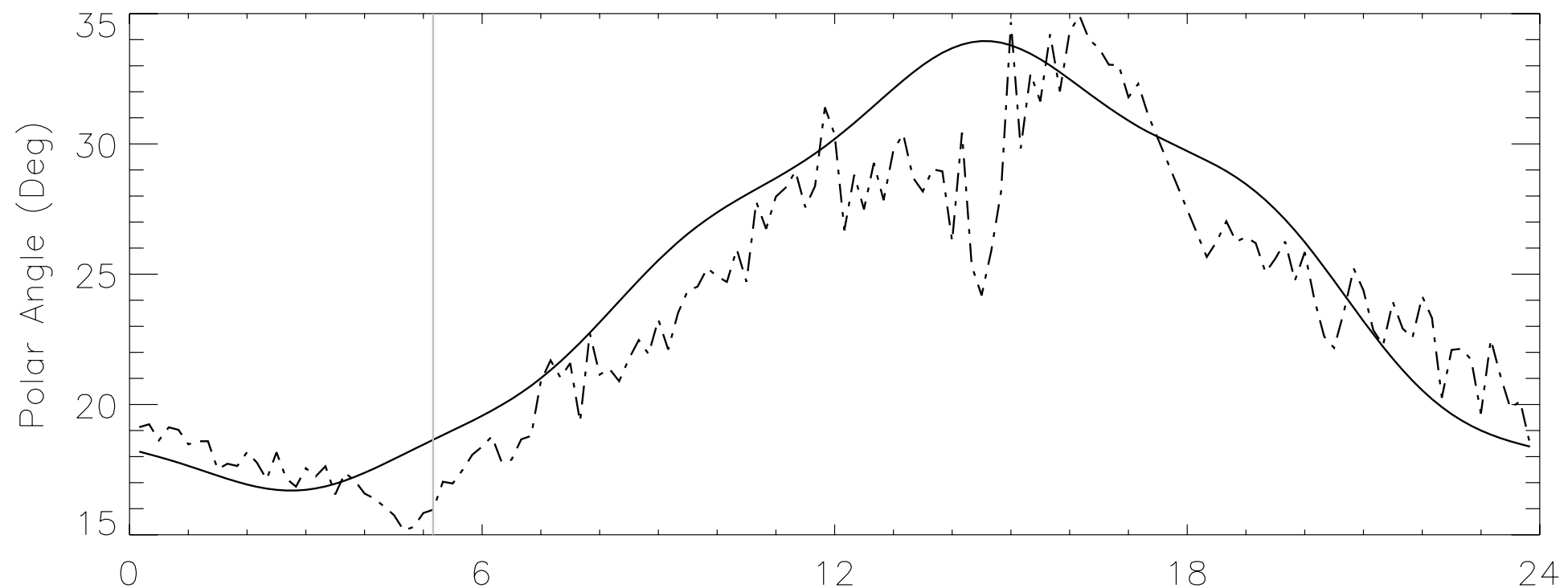
## GOES 3-components, 2 s/c

GOES-10 20021211 Quiet MAG model

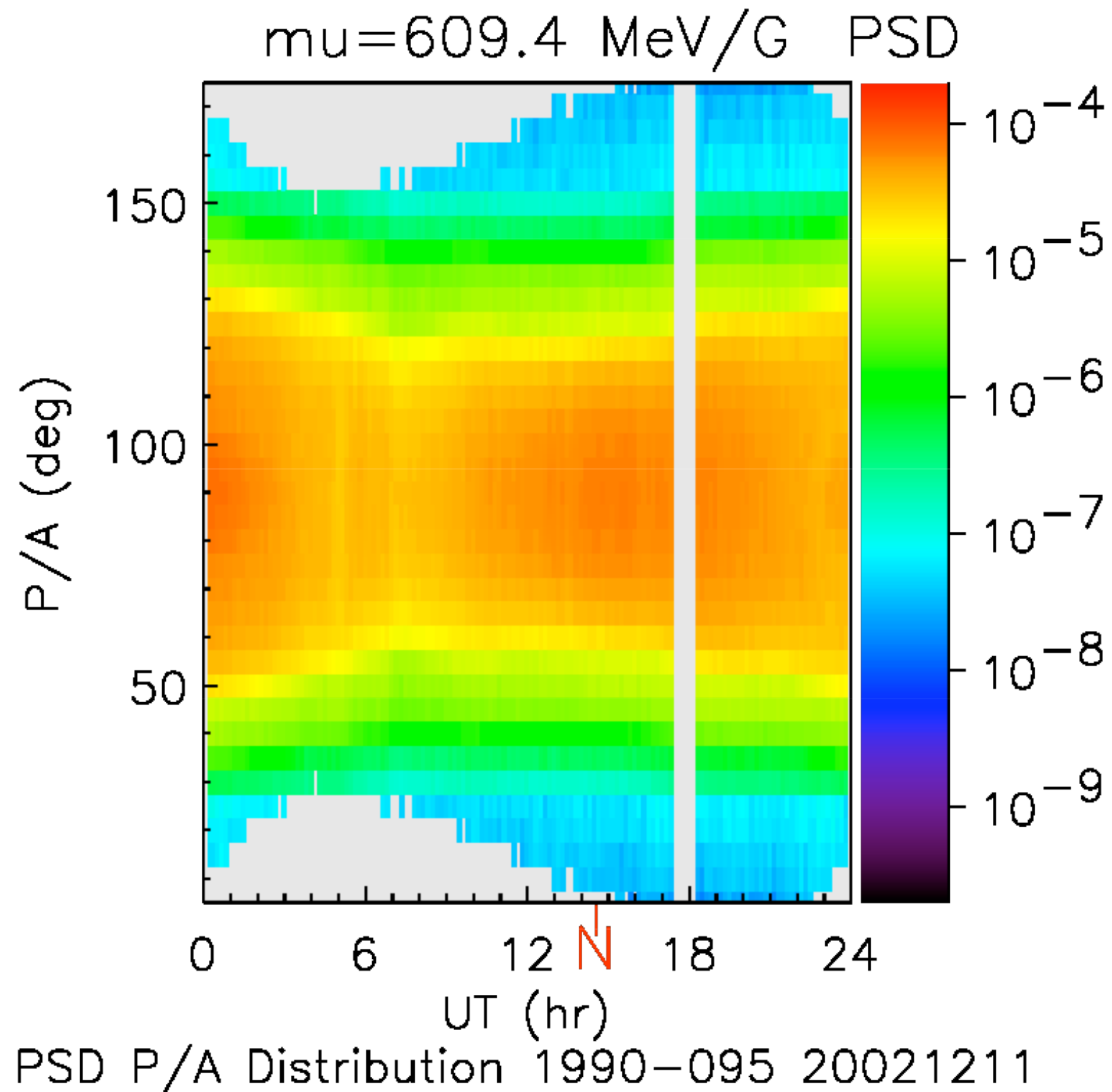


## LANL only $\theta$ and $\Phi$ , but 6 s/c

LANL-97A 20021211 Quiet MAG model

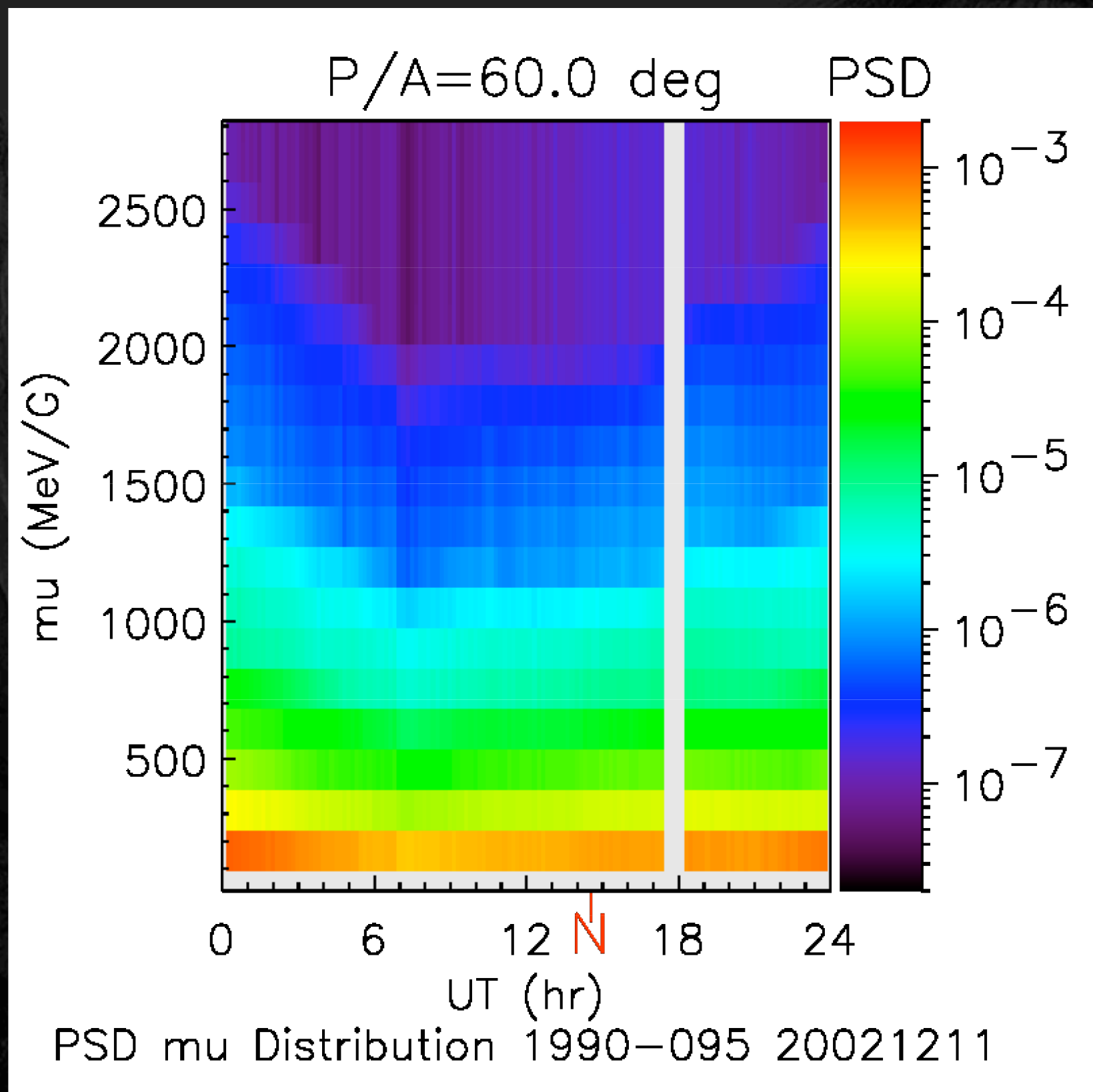


# PSD vs Pitch Angle, fixed $\mu$

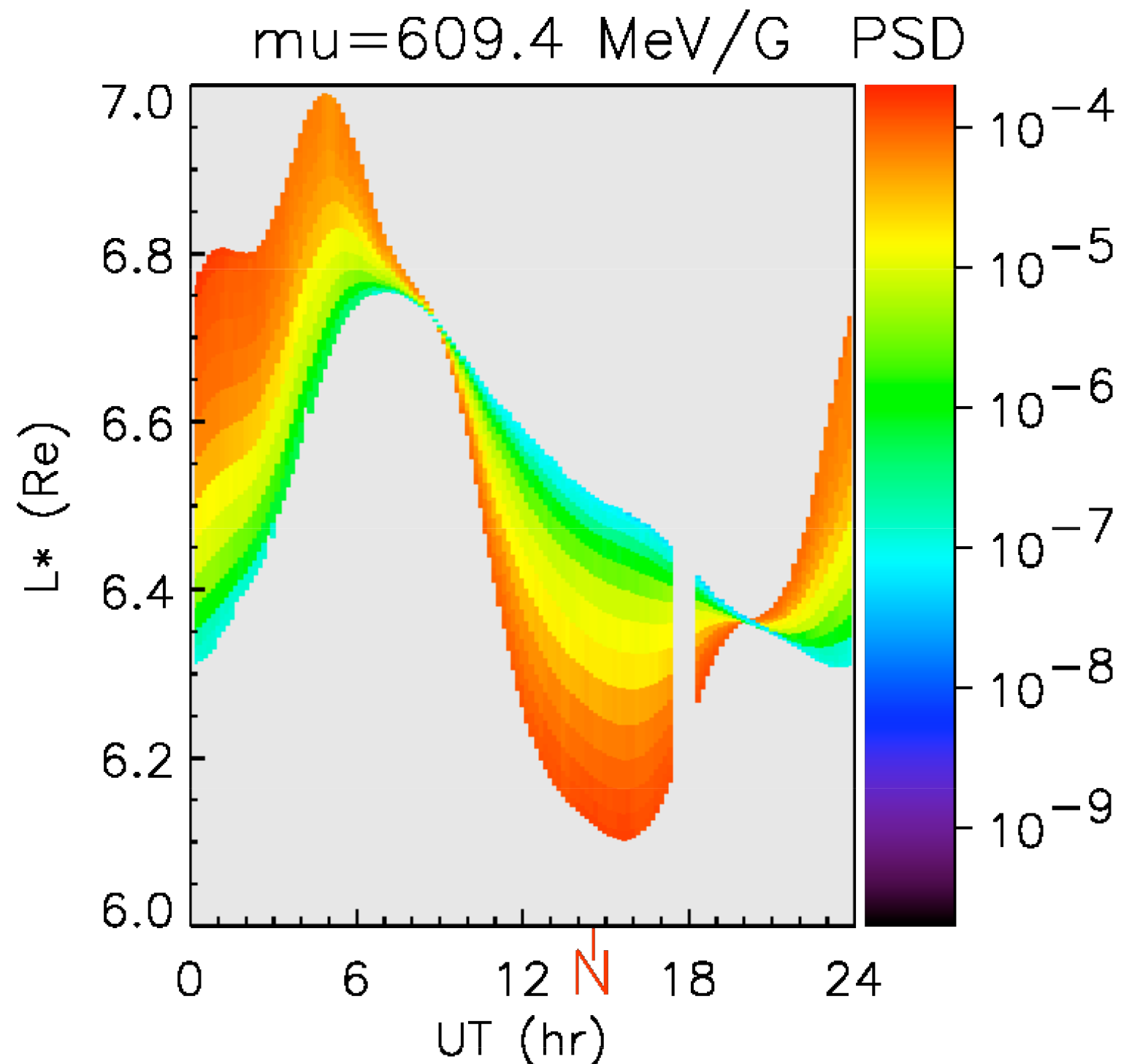




# PSD vs $\mu$ , fixed Pitch Angle



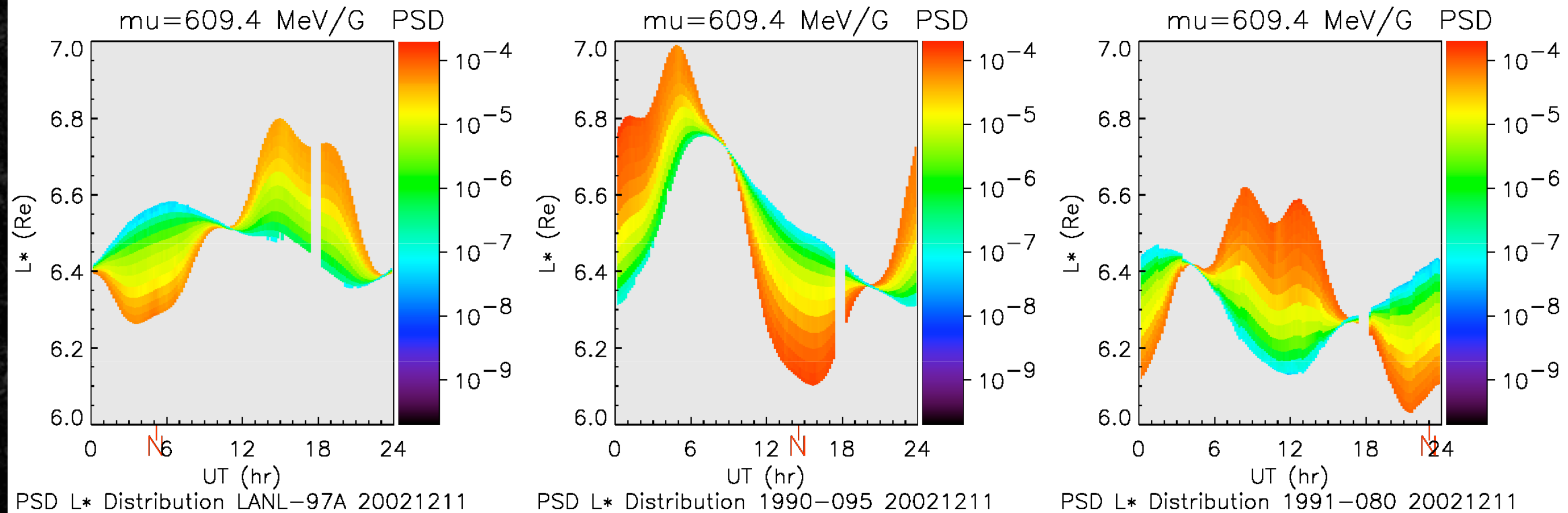
# PSD vs $L^*$ , fixed $\mu$ , J



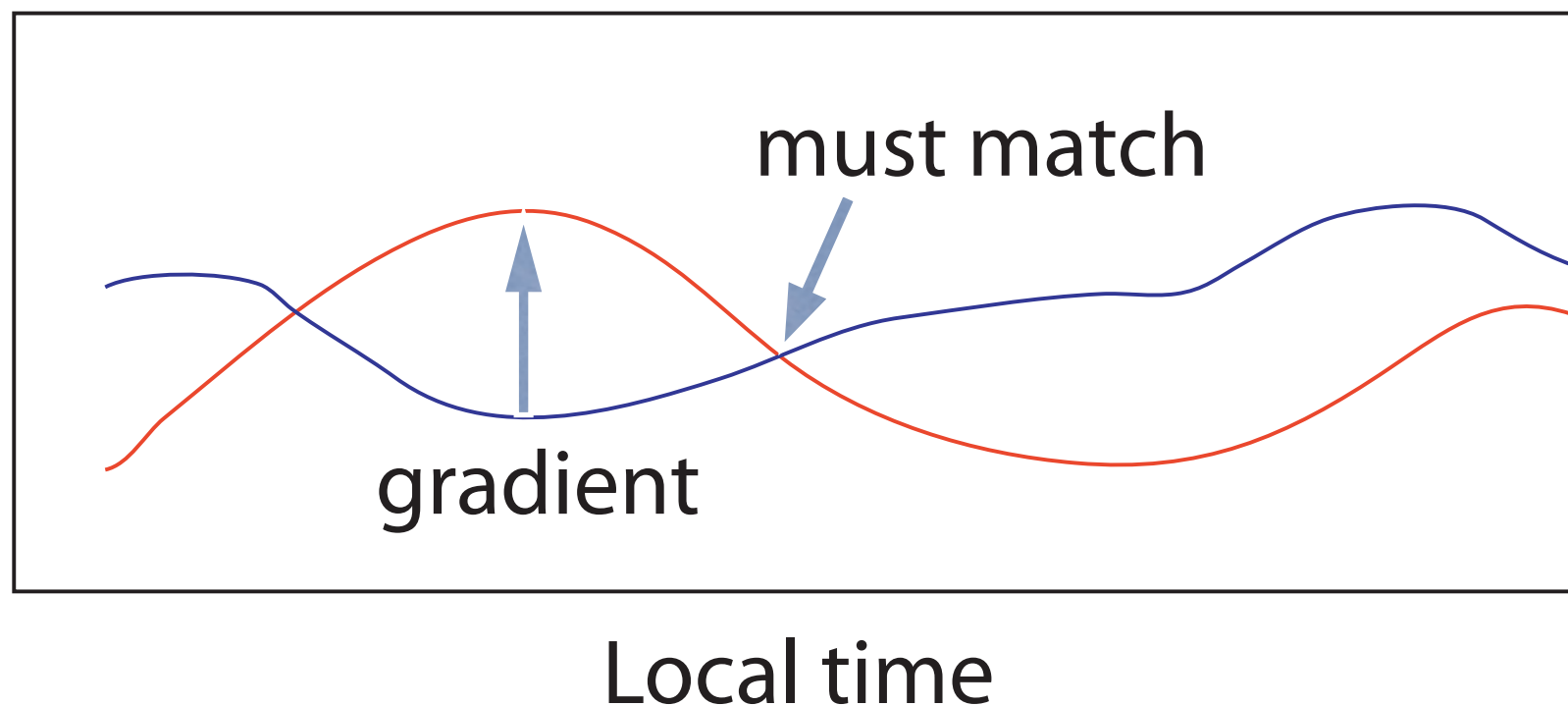
PSD  $L^*$  Distribution 1990–095 20021211



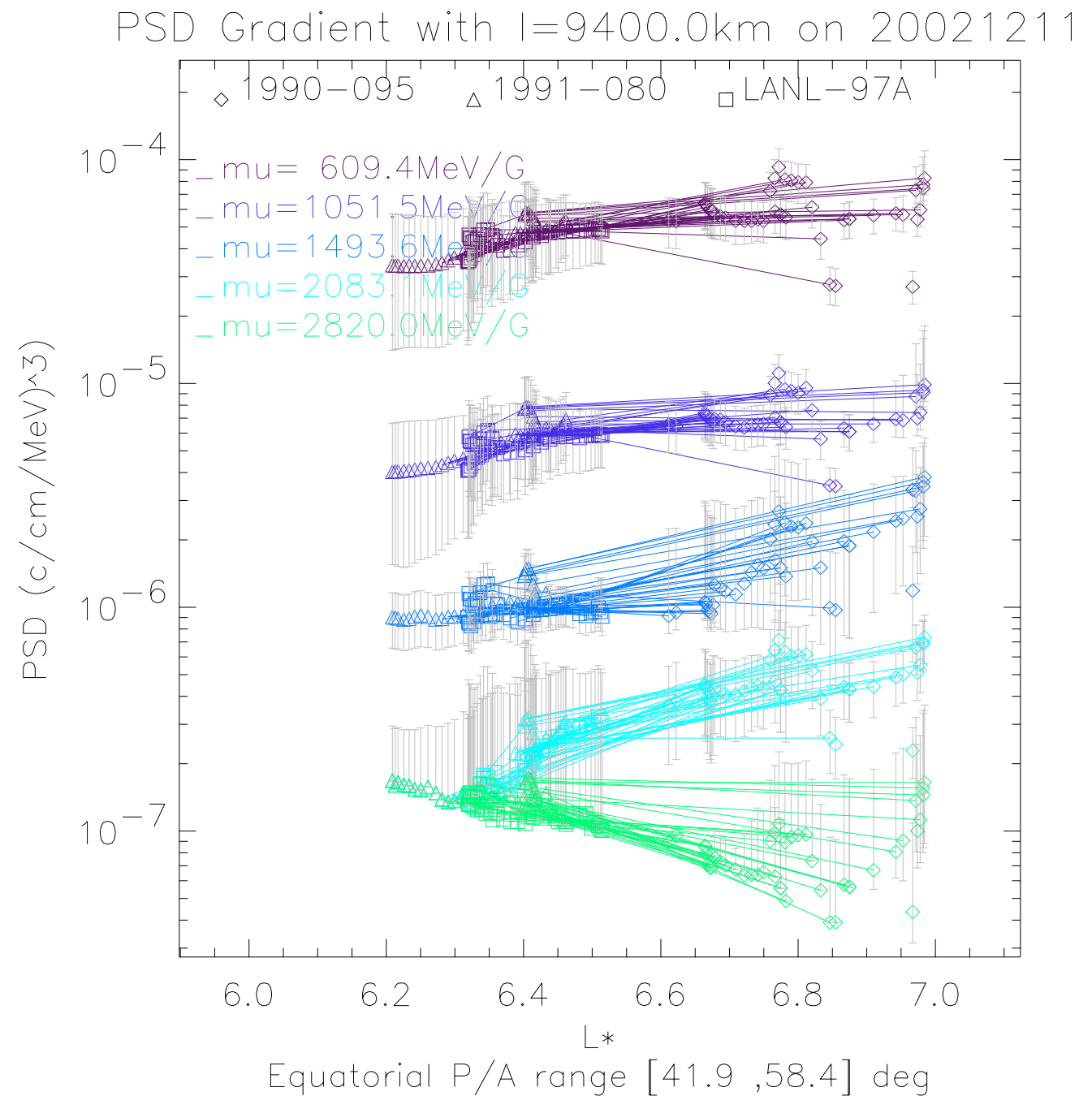
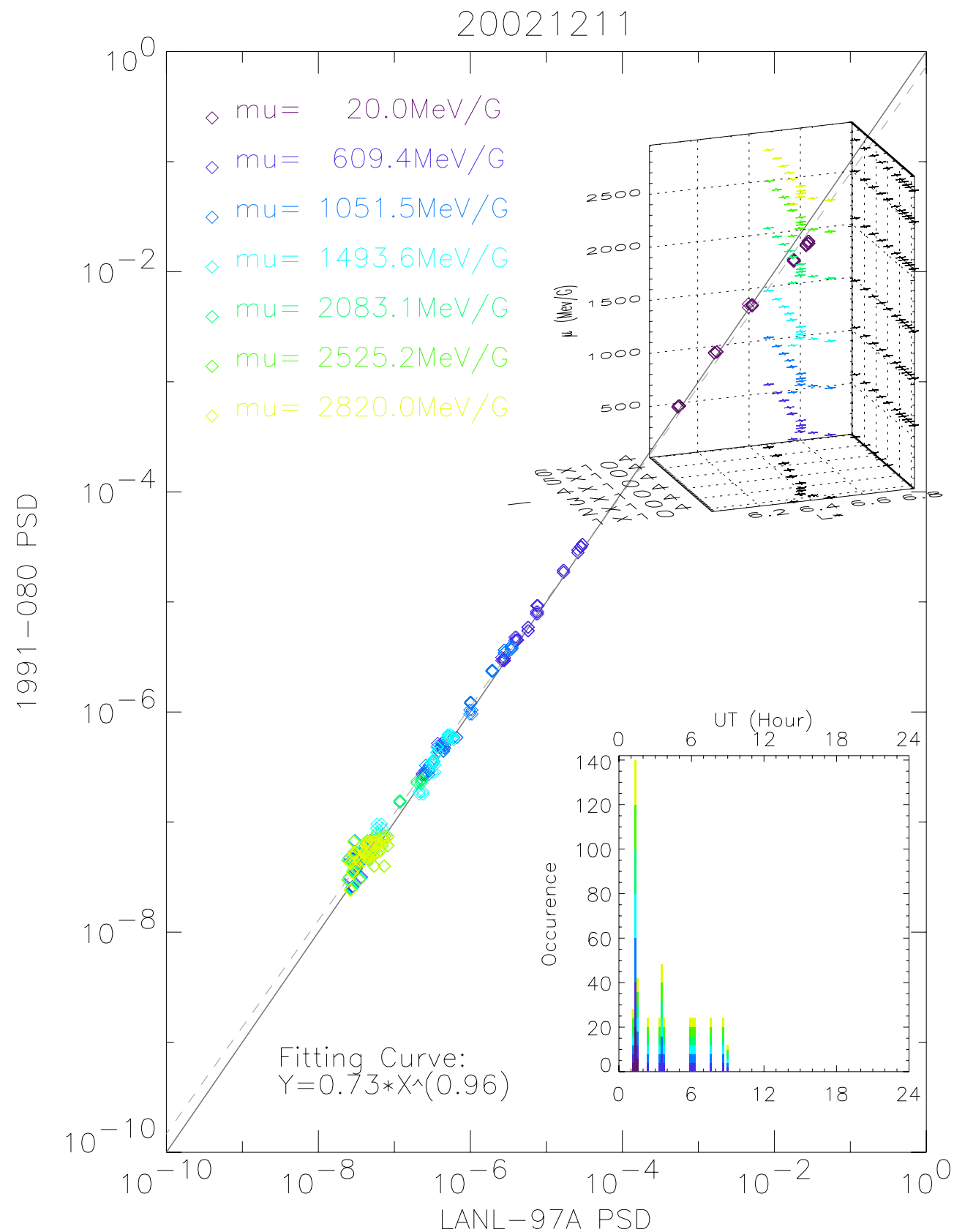
# PSD vs $L^*$ for 3 Satellites



$L^*$  at fixed  $\mu$  and  $J$



# Matching & Gradients



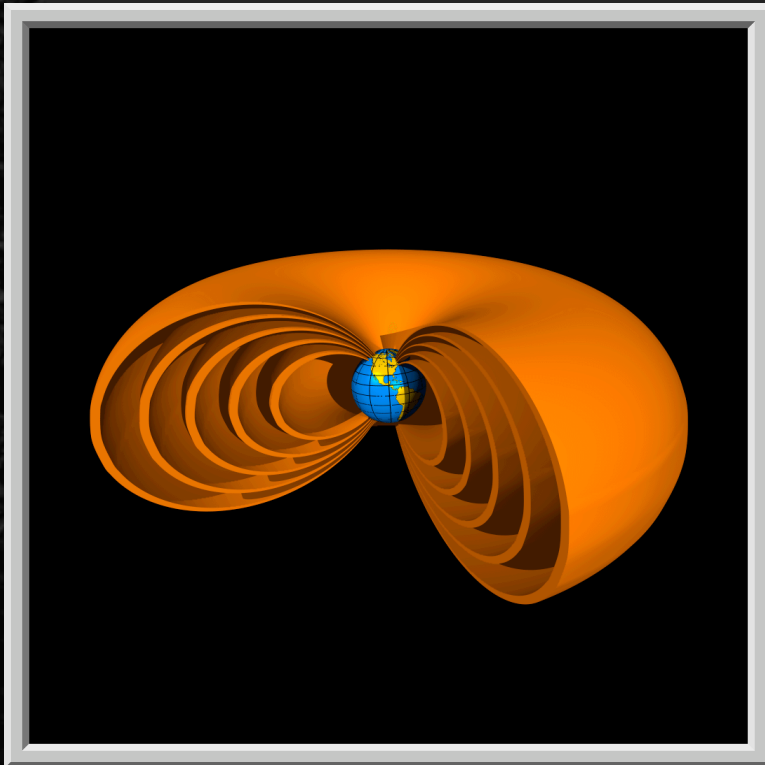


# Next Steps

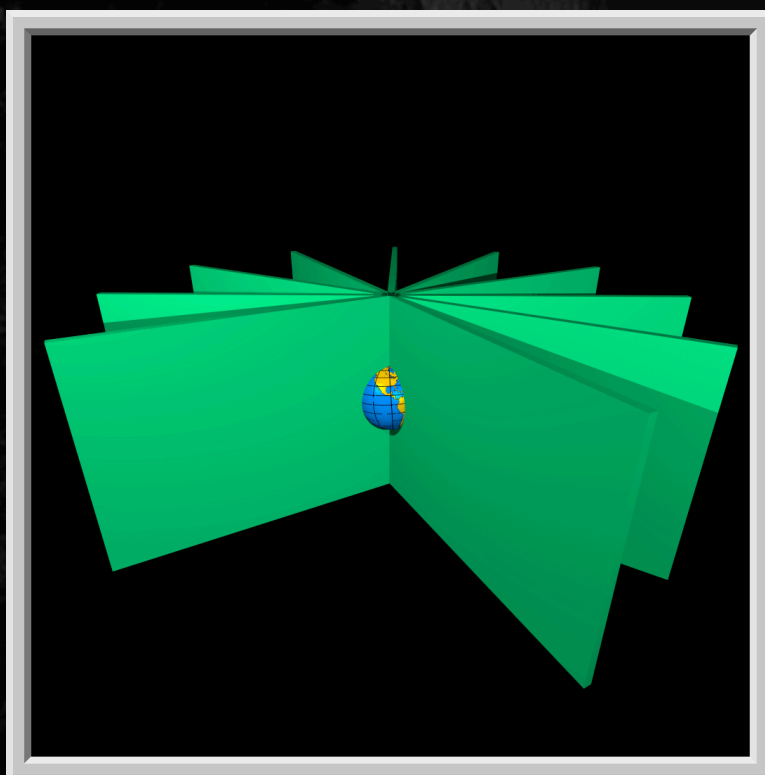
- Allow adjustable, time dependent magnetic field model (e.g. T-01)
- Compare 'real Dst' with Dst determined from GOES & LANL

# Deformable Magnetic Fields

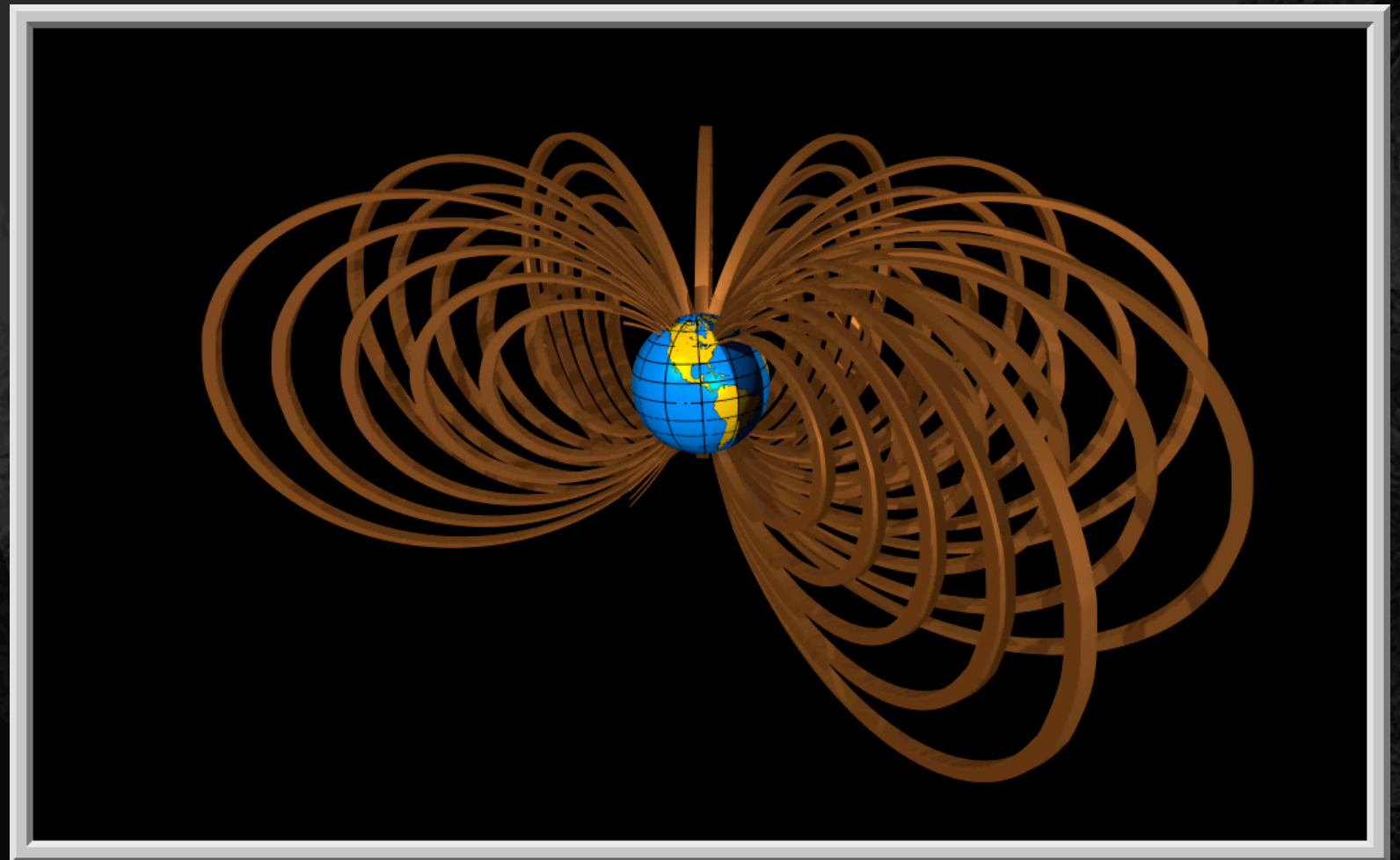
$\alpha = \text{const}$  surfaces



$\beta = \text{const}$  surfaces



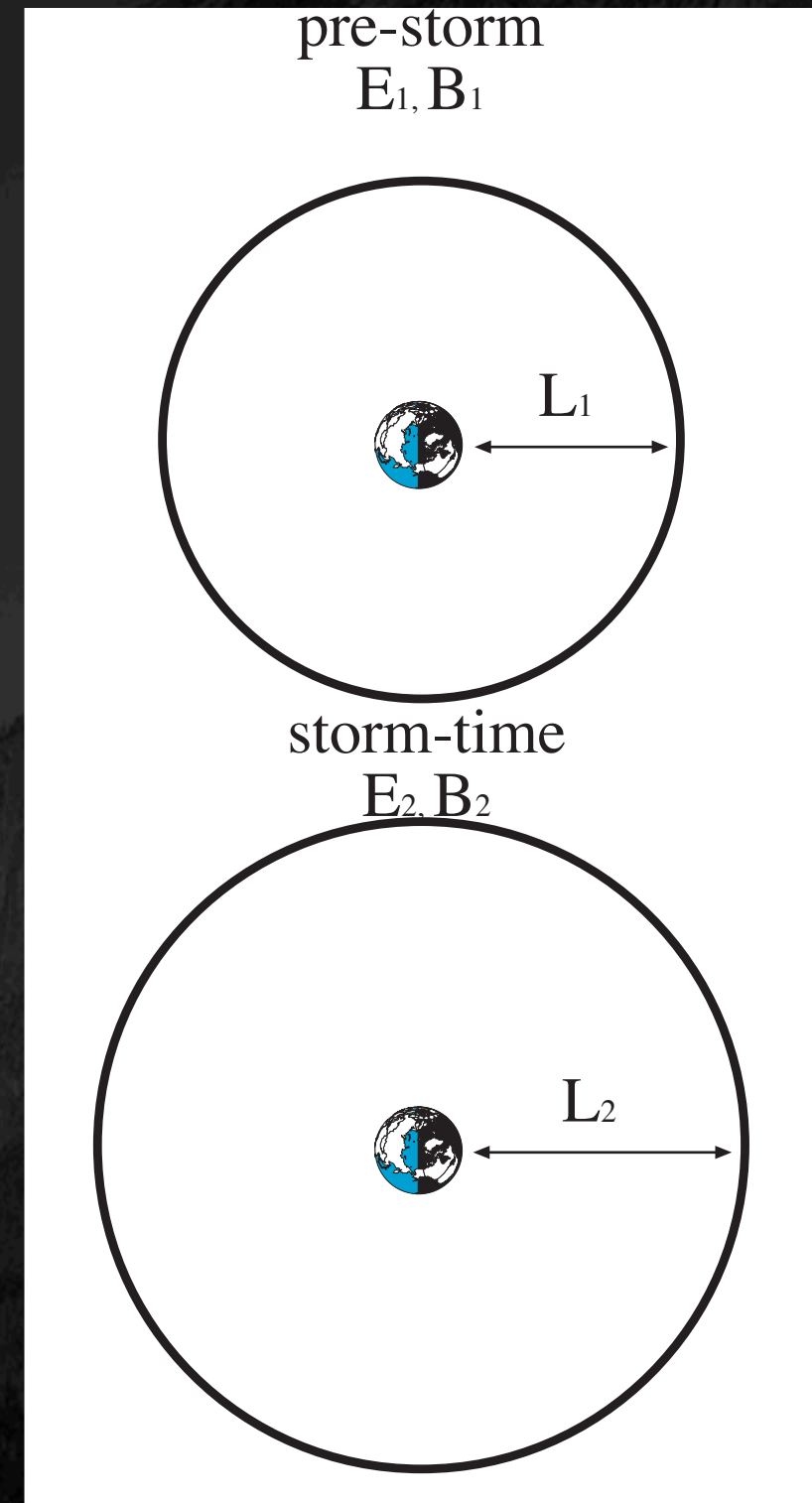
$$\mathbf{B} = \nabla\alpha \times \nabla\beta$$





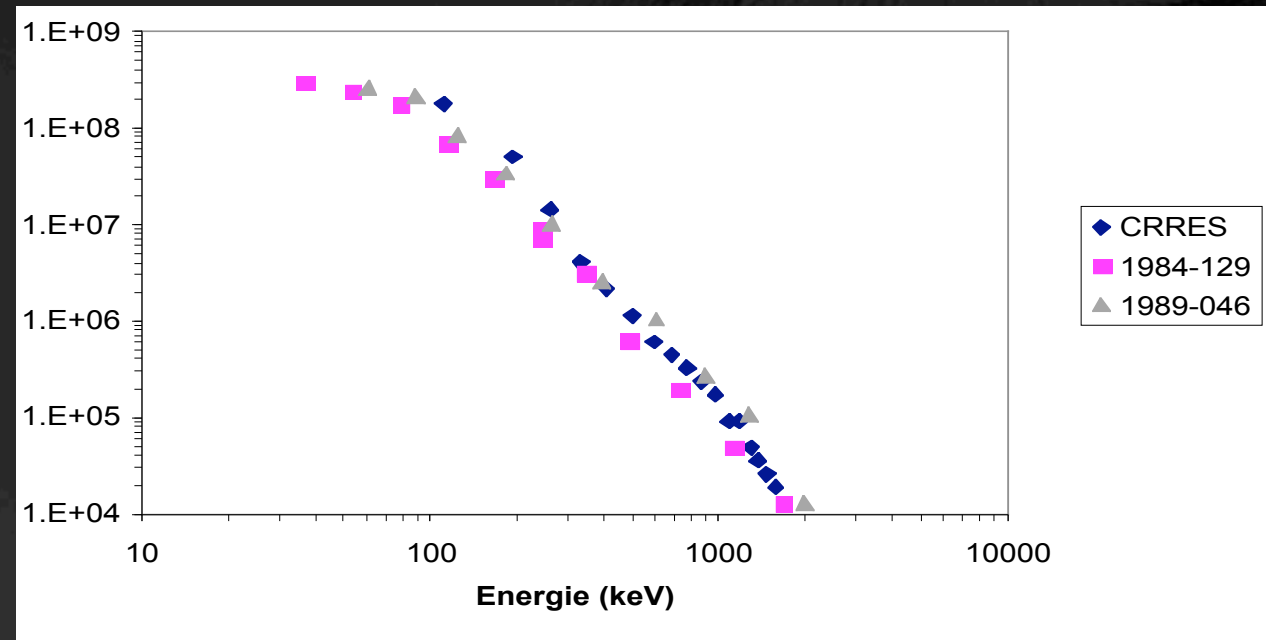
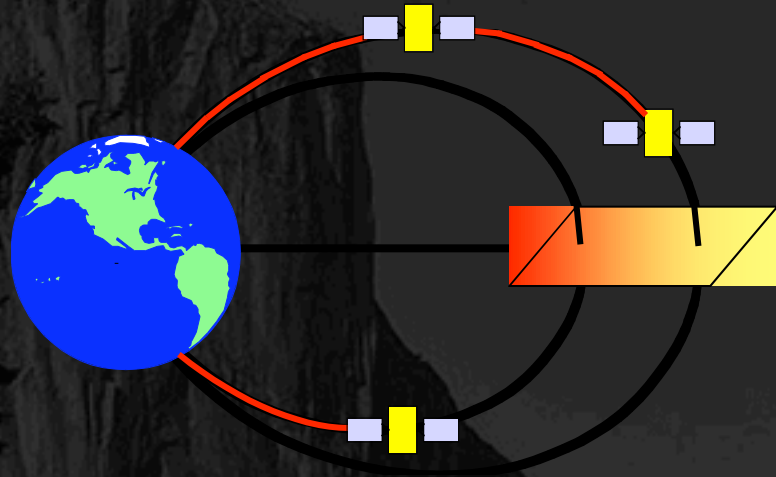
# The 'Dst' Effect

- Must be consistent with particle motion
- Magnitude depends on Dst & Radial Gradient Spectral Slope
- Each new B model changes calculation of  $\mu$ ,  $J$ ,  $L^*$



# Other Challenges

- Satellite Data Intercalibration & other limitations



- Sophisticated but fast, highly-parallel codes

